# Spin transport in topological insulators

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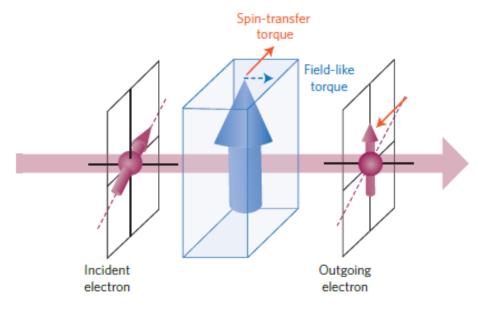
#### Outline

Introduction to spin current and spin transfer torques

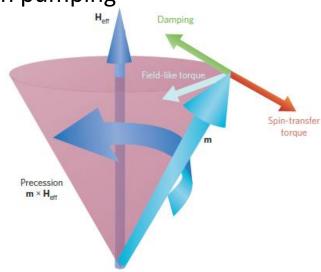
- Measuring spin Hall angle and IEE length
- Spin pumping
- Spin-torque ferromagnetic resonance (ST-FMR)
- Modulation of magnetization damping (MOD)

Spin transport in TIs: paper review

#### Spin transfer torques



Ferromagnetic resonance (FMR)
Spin pumping



A. Brataas, et al., Nat. Mater. **11**, 372 (2012)

LLG equation with torque terms:

$$\frac{\partial \mathbf{m}}{\partial t} = -y\mathbf{m} \times H_{eff} + \alpha \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} + \mathbf{\tau}$$

Damp-like torque:

$$-\frac{\gamma\hbar}{2eM_sV}\mathbf{m}\times(\mathbf{m}\times I_s)$$

Field-like torque:

$$-\frac{\gamma\hbar}{2eM_sV}\mathbf{m}\times I_s$$

#### Spin current

$$\mathbf{Q} = \mathbf{v} \otimes \mathbf{s}$$

$$= \frac{\hbar^2}{2m} \operatorname{Im} (\psi^* \mathbf{\sigma} \otimes \nabla \psi)$$

For a spinor plane-wave wavefunction in x direction:

$$\psi = \frac{e^{ikx}}{\sqrt{\Omega}} \operatorname{Im}(a|\uparrow\rangle + b|\downarrow\rangle)$$

$$Q_{xx} = \frac{\hbar^2 k}{2m\Omega} 2 \operatorname{Re}(ab^*)$$

$$Q_{xy} = \frac{\hbar^2 k}{2m\Omega} 2\operatorname{Im}(ab^*)$$

$$Q_{xz} = \frac{\hbar^2 k}{2m\Omega} 2 \operatorname{Re}(|a|^2 - |b|^2)$$

Conservation of angular momentum Spin transfer torque:

$$\mathbf{N}_{st} = -\int_{pillbox} d^2 R \hat{\mathbf{n}} \cdot \mathbf{Q}$$
$$= -\int_{pillbox} d^3 r \nabla \cdot \mathbf{Q}$$

D. C. Ralph, J. Magn. Magn. Mat. 320, 1190 (2008)

$$\psi_{in} = \frac{e^{ikx}}{\sqrt{\Omega}} \left( \cos(\theta/2) |\uparrow\rangle + \sin(\theta/2) |\downarrow\rangle \right)$$

$$\psi_{trans} = \frac{e^{ikx}}{\sqrt{\Omega}} \left( t_{\uparrow} \cos(\theta/2) |\uparrow\rangle + t_{\downarrow} \sin(\theta/2) |\downarrow\rangle \right)$$

$$\psi_{trans} = \frac{e^{ikx}}{\sqrt{\Omega}} \left( t_{\uparrow} \cos(\theta/2) |\uparrow\rangle + t_{\downarrow} \sin(\theta/2) |\downarrow\rangle \right)$$

$$\psi_{refl} = \frac{e^{-ikx}}{\sqrt{\Omega}} \left( r_{\uparrow} \cos(\theta/2) | \uparrow \rangle + r_{\downarrow} \sin(\theta/2) | \downarrow \rangle \right)$$

$$\mathbf{Q}_{in} = \frac{\hbar^2 k}{2m\Omega} \left[ \sin(\theta) \hat{\mathbf{x}} + \cos(\theta) \hat{\mathbf{z}} \right]$$

$$\mathbf{Q}_{trans} = \frac{\hbar^{2}k}{2m\Omega} \sin(\theta) \operatorname{Re}(t_{\uparrow}t_{\downarrow}^{*}) \hat{\mathbf{x}} + \frac{\hbar^{2}k}{2m\Omega} \sin(\theta) \operatorname{Im}(t_{\uparrow}t_{\downarrow}^{*}) \hat{\mathbf{y}}$$
$$+ \frac{\hbar^{2}k}{2m\Omega} (|t_{\uparrow}|^{2} \cos^{2}(\theta/2) - |t_{\downarrow}|^{2} \sin^{2}(\theta/2)) \hat{\mathbf{z}}$$

$$\mathbf{Q}_{refl} = -\frac{\hbar^{2}k}{2m\Omega}\sin(\theta)\operatorname{Re}\left(r_{\uparrow}r_{\downarrow}^{*}\right)\hat{\mathbf{x}} - \frac{\hbar^{2}k}{2m\Omega}\sin(\theta)\operatorname{Im}\left(r_{\uparrow}r_{\downarrow}^{*}\right)\hat{\mathbf{y}}$$
$$-\frac{\hbar^{2}k}{2m\Omega}\left(\left|r_{\uparrow}\right|^{2}\cos^{2}\left(\theta/2\right) - \left|r_{\downarrow}\right|^{2}\sin^{2}\left(\theta/2\right)\right)\hat{\mathbf{z}}$$

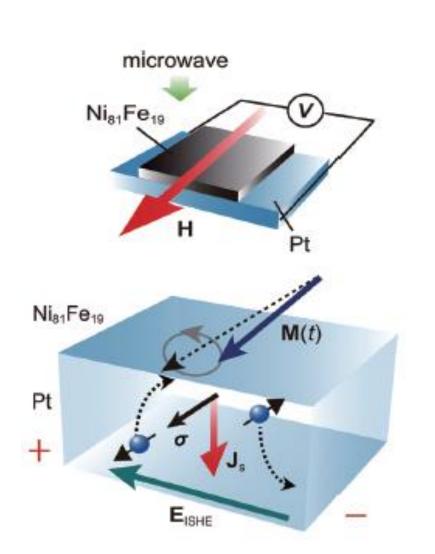
$$(\left|t_{\uparrow}\right|^{2} + \left|r_{\uparrow}\right|^{2} = 1$$

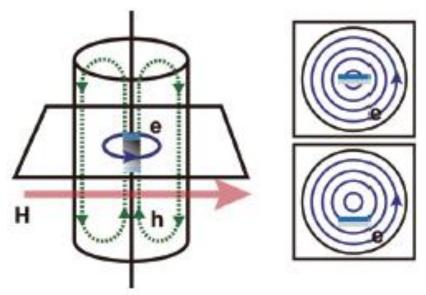
$$\left|t_{\downarrow}\right|^{2} + \left|r_{\downarrow}\right|^{2} = 1$$

Spin mixing conductance

$$\begin{pmatrix} a' \\ b' \end{pmatrix} = \begin{pmatrix} G_{\uparrow \uparrow} & G_{\uparrow \downarrow} \\ G_{\downarrow \uparrow}^* & G_{\downarrow \downarrow} \end{pmatrix} \begin{pmatrix} a \\ b \end{pmatrix} \operatorname{Re}(G_{\uparrow \downarrow}) >> \operatorname{Im}(G_{\uparrow \downarrow}) \text{ for metals}$$

## Spin pumping



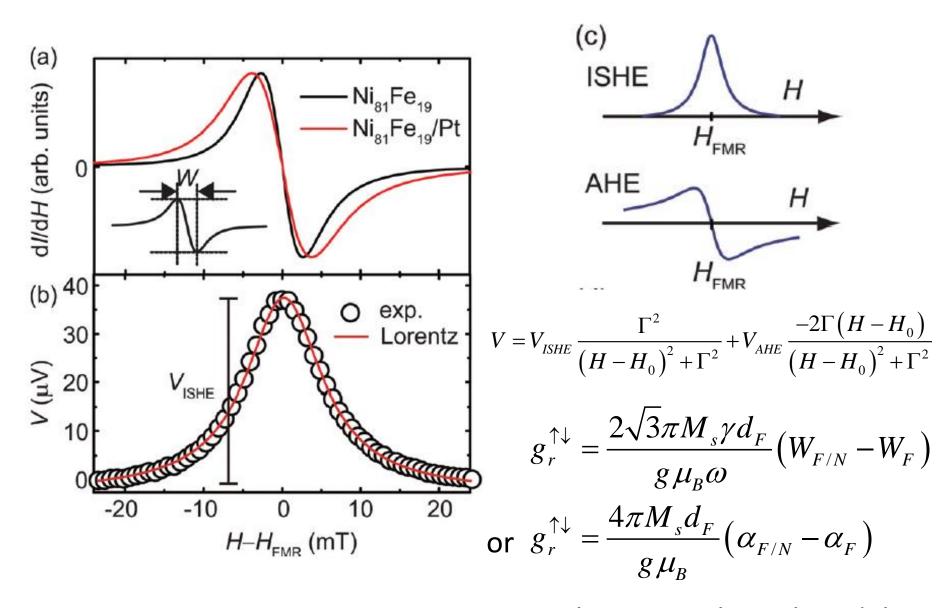


Spin current projected along H<sub>ext</sub>:

$$j_s = \frac{\omega}{2\pi} \int_0^{2\pi/\omega} \frac{\hbar}{4\pi} g_r^{\uparrow\downarrow} \frac{1}{M_s^2} \left[ \mathbf{M}(t) \times \frac{d\mathbf{M}(t)}{dt} \right]_z dt$$

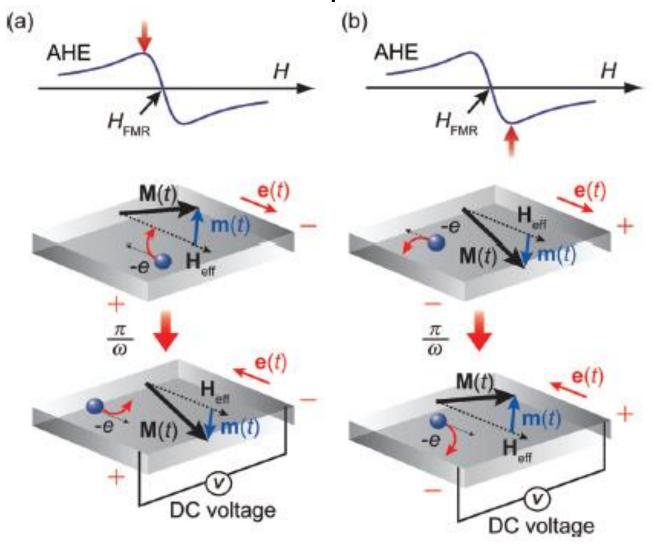
$$V_{\rm ISHE} \propto \boldsymbol{J}_{\rm c} \propto \theta_{\rm SH} \boldsymbol{J}_{\rm s} \times \boldsymbol{\sigma} \propto \theta_{\rm SH} \boldsymbol{J}_{\rm s} \times \boldsymbol{M}$$
  
  $\propto \theta_{\rm SH} \boldsymbol{J}_{\rm s} \times \boldsymbol{H} \propto \theta_{\rm SH} \sin \theta_{\rm H},$ 

K. Ando, J. Appl. Phys. 109, 103913 (2011)



A phenomenological model

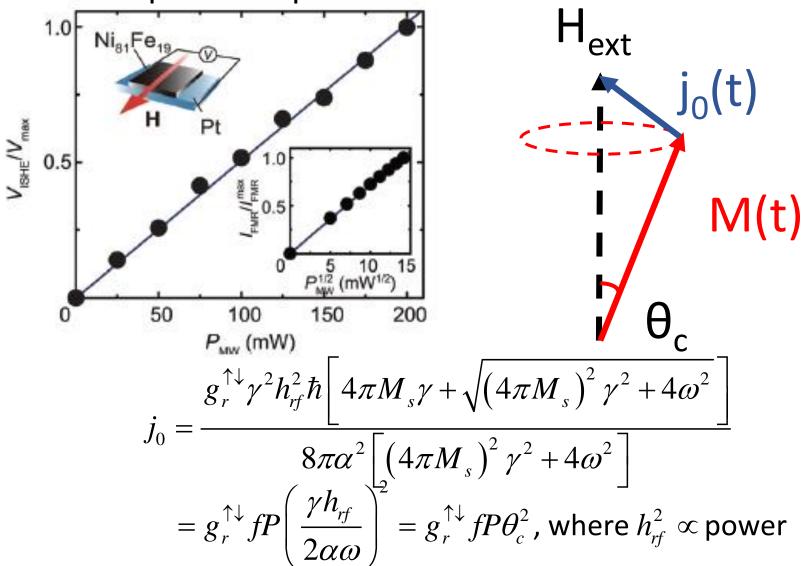
#### Antisymmetric lineshape from AHE or AMR



Phase shift between the microwave and magnetization determine the polarity.

## Small cone angle (linear) regime

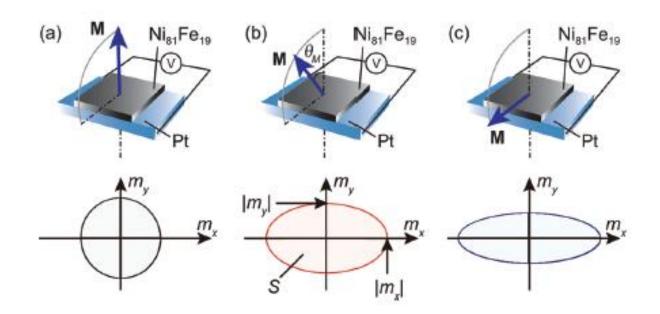
Linear power dependence



#### The P factor

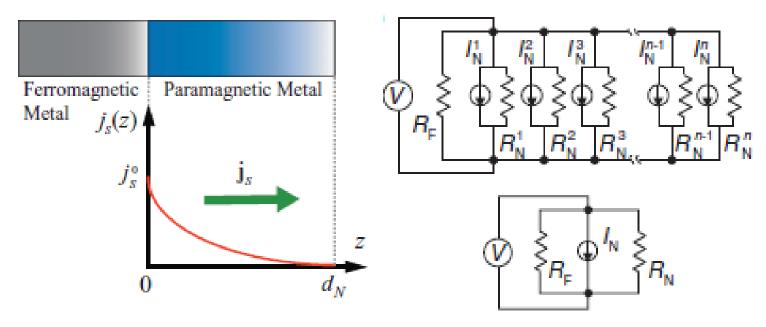
$$P = \frac{2\omega \left[ 4\pi M_{s} \gamma + \sqrt{(4\pi M_{s})^{2} \gamma^{2} + 4\omega^{2}} \right]}{(4\pi M_{s})^{2} \gamma^{2} + 4\omega^{2}}$$

can be viewed as a correction factor.



The pumped spin current is proportional to the trajectory area. Spin pumping is an adiabatic process. (think about the Carnot engine.)

## Spin distribution in normal metals

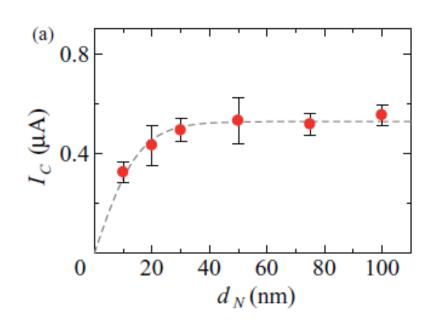


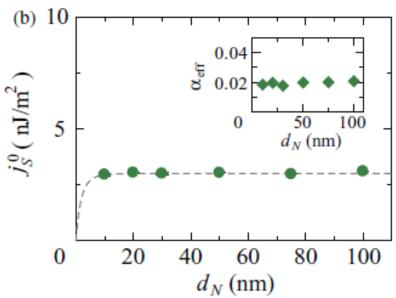
Spin Hall effect acts as a charge current source.

Solving the spin diffusion equation...

$$j_{s}(z) = \frac{\sinh\left[\left(d_{N}-z\right)/\lambda_{N}\right]}{\sinh\left(d_{N}/\lambda_{N}\right)} j_{s}^{0}$$

## Thickness dependence





Spin backflow depends on the spin diffusion length.

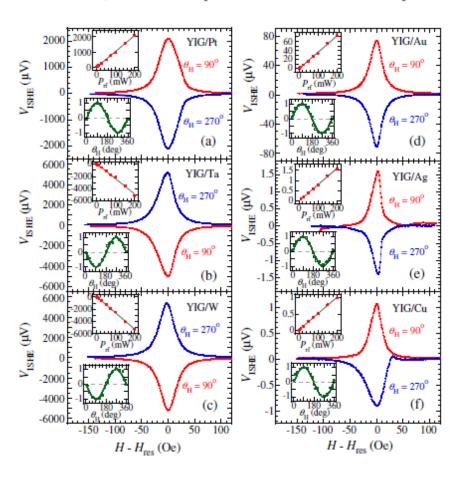
$$\langle j_c \rangle = \frac{1}{d_N} \int_0^{d_N} j_c(y) dy$$

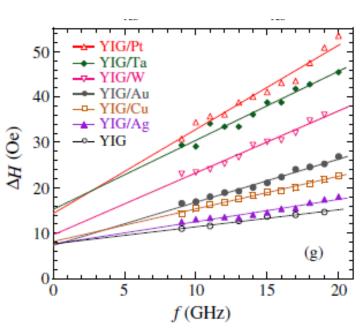
$$= \theta_{SH} \left( \frac{2e}{\hbar} \right) \frac{\lambda_N}{d_N} \tanh \left( \frac{d_N}{2\lambda_N} \right) j_s^0$$

Need to get the thickness dependence data to calculate the spin Hall angle

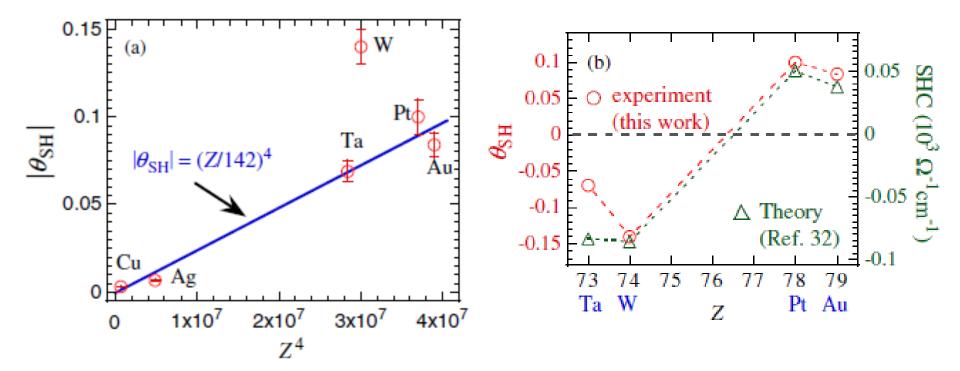
#### Scaling of Spin Hall Angle in 3d, 4d, and 5d Metals from Y<sub>3</sub>Fe<sub>5</sub>O<sub>12</sub>/Metal Spin Pumping

H. L. Wang, <sup>1</sup> C. H. Du, <sup>1</sup> Y. Pu, <sup>1</sup> R. Adur, <sup>1</sup> P. C. Hammel, <sup>1,\*</sup> and F. Y. Yang <sup>1,†</sup> <sup>1</sup>Department of Physics, The Ohio State University, Columbus, Ohio 43210, USA (Received 23 September 2013; revised manuscript received 24 December 2013; published 15 May 2014)





Bilayer	$V_{ m ISHE}$	$\Delta H$ change	$lpha_{ m sp}$	$\rho(\Omega m)$	$g_{\uparrow\downarrow}(\mathrm{m}^{-2})$	$\lambda_{SD}(nm)$	$ heta_{ ext{SH}}$	$J_s(A/m^2)$
YIG/Pt	2.10 mV	24.3 Oe	$(3.6 \pm 0.3) \times 10^{-3}$	$4.8 \times 10^{-7}$	$(6.9 \pm 0.6) \times 10^{18}$	7.3	$0.10 \pm 0.01$	$(2.0 \pm 0.2) \times 10^7$
YIG/Ta	-5.10 mV	16.5 Oe	$(2.8 \pm 0.2) \times 10^{-3}$	$2.9 \times 10^{-6}$	$(5.4 \pm 0.5) \times 10^{18}$	1.9	$-0.071 \pm 0.006$	$(1.6 \pm 0.2) \times 10^7$
YIG/W	-5.26 mV	12.3 Oe	$(2.4 \pm 0.2) \times 10^{-3}$			2.1	$-0.14 \pm 0.01$	$(1.4 \pm 0.1) \times 10^7$
YIG/Au	$72.6 \mu V$	5.50 Oe	$(1.4 \pm 0.1) \times 10^{-3}$	$4.9 \times 10^{-8}$	$(2.7 \pm 0.2) \times 10^{18}$	60	$0.084 \pm 0.007$	$(7.6 \pm 0.7) \times 10^6$
YIG/Ag	1.49 $\mu V$	1.30 Oe	$(2.7 \pm 0.2) \times 10^{-4}$	$6.6 \times 10^{-8}$	$(5.2 \pm 0.5) \times 10^{17}$	700	$0.0068 \pm 0.0007$	$(1.5 \pm 0.1) \times 10^6$
YIG/Cu	$0.99 \mu V$	3.70 Oe	$(8.1 \pm 0.6) \times 10^{-4}$	$6.3 \times 10^{-8}$	$(1.6 \pm 0.1) \times 10^{18}$	500	$0.0032 \pm 0.0003$	$(4.6 \pm 0.4) \times 10^6$



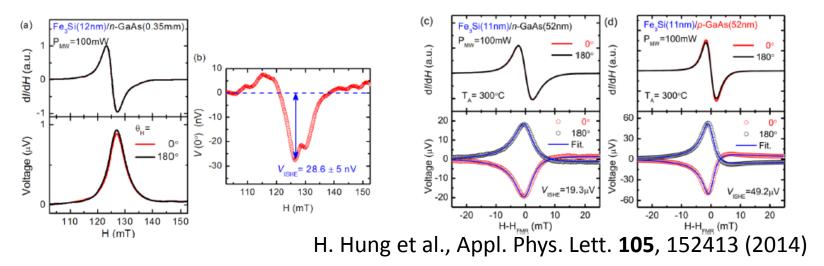
Spin Hall angles strongly depend on the d-electron count.

	T(K)	λ <sub>sd</sub> (nm)	σ <sub>NM</sub> (10 <sup>6</sup> S/m)	α <sub>SH</sub> (%)		T(K)	λ <sub>sd</sub> (nm)	$\sigma_{\rm NM} \; (10^6 \; {\rm S/m})$	α <sub>SH</sub> (%)
Al	4,2	$455 \pm 15$	10.5	$0.032 \pm 0.006$	Мо	10	10	3.03	-0.20
	4.2	$705 \pm 30$	17	$0.016 \pm 0.004$		10	10	0.667	-0.075
Au	295	$86 \pm 10$	37	11.3		10	$8.6 \pm 1.3$	2.8	$-(0.8 \pm 0.18)$
	295	83	37	3		295	$35 \pm 3^{*}$	4.66	$-(0.05 \pm 0.01)$
	4.5	65*	48.3	<2.3	Nb	10	$5.9 \pm 0.3$	1.1	$-(0.87 \pm 0.20)$
	295	36*	25.7	<2.7	Pd	10	$13 \pm 2$	2.2	$1.2 \pm 0.4$
	295	$35 \pm 4$	28	$7.0 \pm 0.1$		295	9*	1.97	1.0
	295	$27 \pm 3$	14	$7.0 \pm 0.3$		295	15 ± 4*	4.0	$0.64 \pm 0.10$
	295	$25 \pm 3$	14.5	$12 \pm 4$		295	$5.5 \pm 0.5$	5	$1.2 \pm 0.3$
	295	$50 \pm 8$	16.7	$0.8 \pm 0.2$		295	$2.0 \pm 0.1$	3.7	$0.8 \pm 0.20$
	<10	$40 \pm 16$	25	$1.4 \pm 0.4$	Pt	295		6.41	0.37
	295	$35 \pm 3^{*}$	25.2	$0.35 \pm 0.03$	rt	5	8	8.0	0.44
	295	35	20	$0.25 \pm 0.1$		295	7	5.56	0.9
	295	$35 \pm 3^{*}$	5.25	$1.6 \pm 0.1$		10	$11 \pm 2$	8.1	$2.1 \pm 0.5$
	295	$35 \pm 3*$	7	$0.335 \pm 0.006$		10	~10	8.1	2.4
	295	35*		$1.1 \pm 0.3$		295	7*	6.4	8.0
	295	60	20.4	$8.4 \pm 0.7$		295	$10 \pm 2^{*}$	2.4	$1.3 \pm 0.2$
AuW	295	1.9	1.75	>10		295	10*	2	4.0
Ag	295	700	15	$0.7 \pm 0.1$		295	$3.7 \pm 0.2$	2,42	$8 \pm 1$
						295	$8.3 \pm 0.9$	$4.3 \pm 0.2$	$1.2 \pm 0.2$
Bi	3	$0.3 \pm 0.1$	-	>0.3		295	$7.7 \pm 0.7$	$1.3 \pm 0.1$	$1.3 \pm 0.1$
	295	-	$2.4 \pm 0.3(I)$	$-(7.1 \pm 0.8)(I)$		295	$1.5 - 10^{\circ}$	$2.45 \pm 0.1$	3+4
			$50 \pm 12(V)$	$1.9 \pm 0.2(V)$		295	4	4	$2.7 \pm 0.5$
Cu	295	500	16	$0.32 \pm 0.03$		295	8 ± 1*	1.02	$2.012 \pm 0.003$
CuIr	10	5-30		$2.1 \pm 0.6$		295	1.3*	2.4	2.1 ± 1.5
	10	3-30		0.7(Ta); 2.6(Ir)		295	1.2 1.4*		$8.6 \pm 0.5$ $12 \pm 4$
CuMn <sub>x</sub> T <sub>y</sub>						295 295	$3.4 \pm 0.4$	6.0	$5.6 \pm 0.1$
				1.35(Au); 1.15(Sb) -1.2(Lu)		295	7.3	2.1	10 ± 1
C.B.		100 20		-1.2(Lu)		295	$1.2 \pm 0.1$	3.6	2.2 ± 0.4

- 1. The larger spin Hall angles, the shorter spin diffusion lengths.
- 2. Depending on techniques, materials preparation and geometry, the calculated spin Hall angle can vary by 1 order of magnitude.
- 3. Rashba effect (broken inversion symmetry) at the interface adds complexity to analyses.

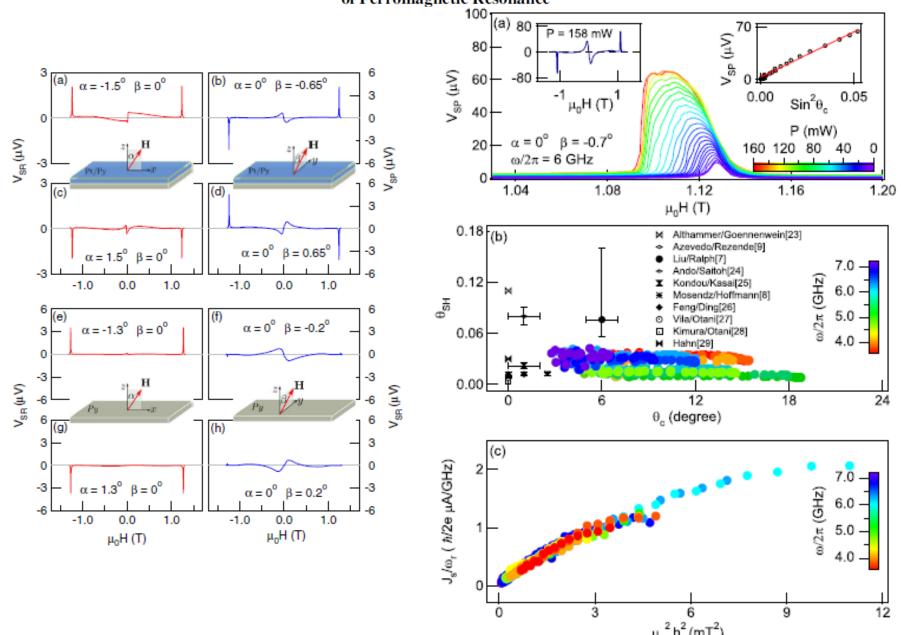
## Spurious effects

• Microwave induced Seebeck effect in semiconductor.



- Spin rectification effect. (can be prevented by YIG)
- the boundary conditions, phase shift between E and B field can strongly affect voltage signals.
- Self-induced ISHE and spin backflow. (can be prevented by YIG)

#### Universal Method for Separating Spin Pumping from Spin Rectification Voltage of Ferromagnetic Resonance



#### Spin-torque ferromagnetic resonance (ST-FMR)

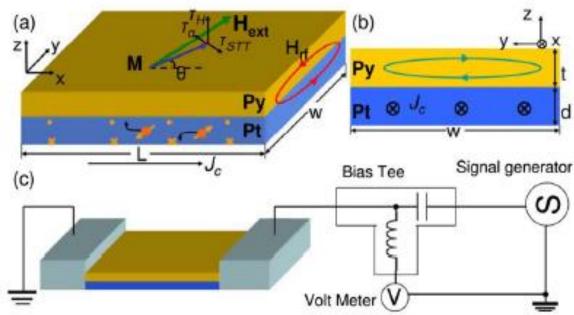
PRL 106, 036601 (2011)

PHYSICAL REVIEW LETTERS

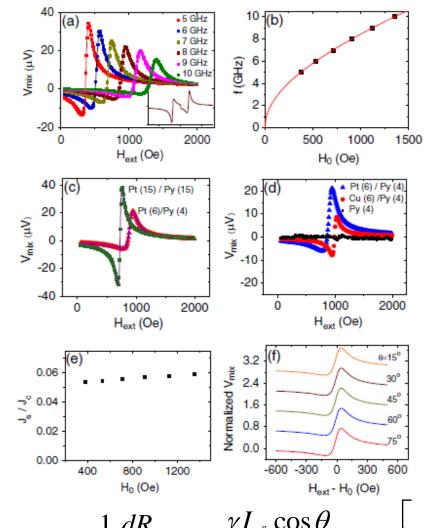
week ending 21 JANUARY 2011

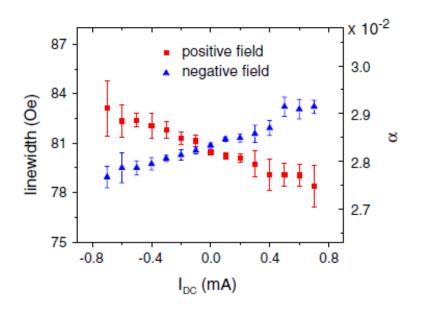
#### Spin-Torque Ferromagnetic Resonance Induced by the Spin Hall Effect

Luqiao Liu, Takahiro Moriyama, D. C. Ralph, and R. A. Buhrman Cornell University, Ithaca, New York, 14853 (Received 12 October 2010; published 20 January 2011)



$$\frac{d\hat{m}}{dt} - \gamma \hat{m} \times \vec{H}_{eff} + \alpha \hat{m} \times \frac{d\hat{m}}{dt} + \gamma \frac{\hbar}{2e\mu_0 M_S t} J_{S,rf} \left( \hat{m} \times \hat{\sigma} \times \hat{m} \right) - \gamma \hat{m} \times \vec{H}_{rf}$$
Anti-damp torques





on AMR to generate voltage signals. Not suitable for magnetic insulator.

Special case: Pt/YIG, Ta/YIG...

$$V_{mix} = -\frac{1}{4} \frac{dR}{d\theta} \frac{\gamma I_{rf} \cos \theta}{\Delta 2\pi \left(df / dH\right)|_{H_{ext} = H_0}} \left[ S \frac{\Delta^2}{\Delta^2 + \left(H_{ext} - H_0\right)^2} + A \frac{\left(H_{ext} - H_0\right)\Delta}{\Delta^2 + \left(H_{ext} - H_0\right)^2} \right]$$

$$\frac{J_{S,rf}}{J_{C,rf}} = \frac{S}{A} \frac{e\mu_0 M_S td}{\hbar} \left[ 1 + \left(4\pi M_{eff} / H_{ext}\right) \right]^{1/2} \text{ The spin Hall angle can be determined from the relative magnitude of the two}$$

components.

## Modulation of magnetization damping (MOD)

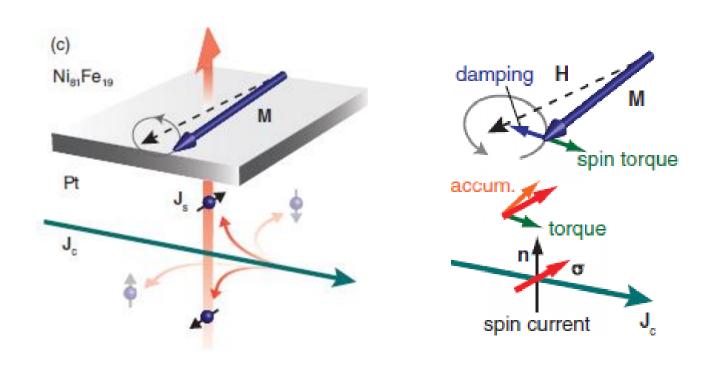
PRL 101, 036601 (2008)

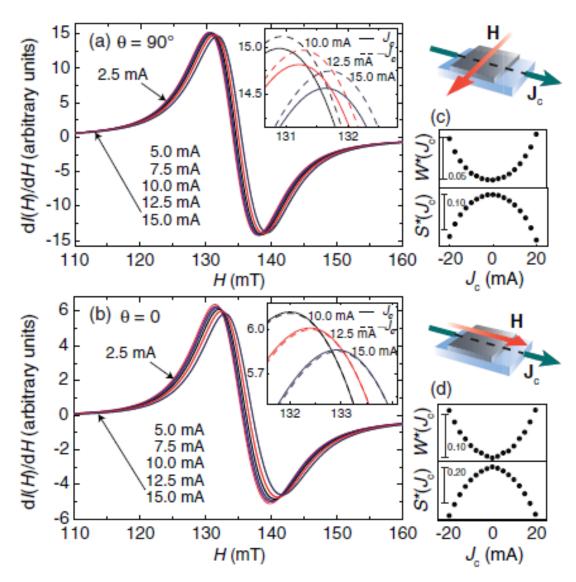
PHYSICAL REVIEW LETTERS

week ending 18 JULY 2008

#### Electric Manipulation of Spin Relaxation Using the Spin Hall Effect

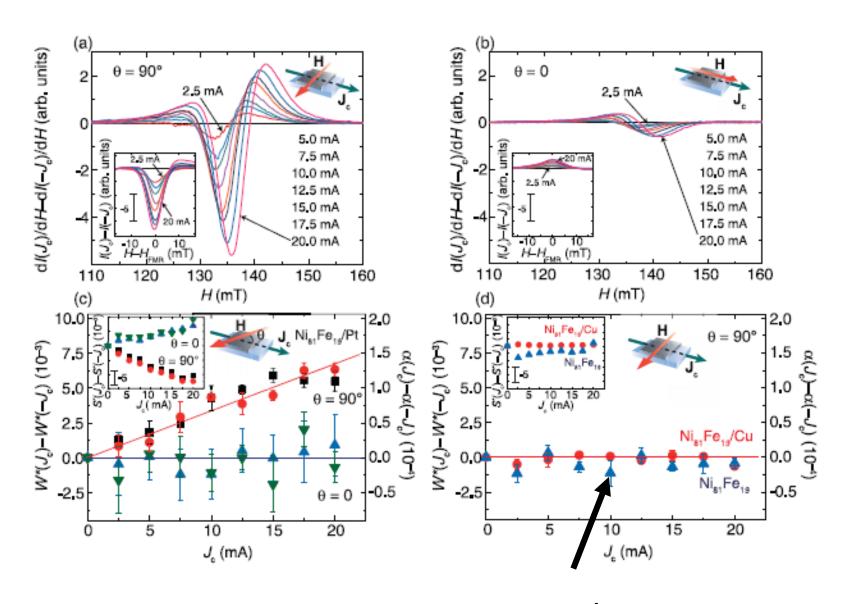
K. Ando, <sup>1,\*</sup> S. Takahashi, <sup>2,3</sup> K. Harii, <sup>1</sup> K. Sasage, <sup>1</sup> J. Ieda, <sup>2,3</sup> S. Maekawa, <sup>2,3</sup> and E. Saitoh <sup>1,4</sup> <sup>1</sup>Department of Applied Physics and Physico-Informatics, Keio University, Yokohama 223-8522, Japan <sup>2</sup>Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan <sup>3</sup>CREST, Japan Science and Technology Agency, Kawaguchi, Saitama 332-0012, Japan <sup>4</sup>PRESTO, Japan Science and Technology Agency, Kawaguchi, Saitama 332-0012, Japan (Received 17 March 2008; published 18 July 2008)



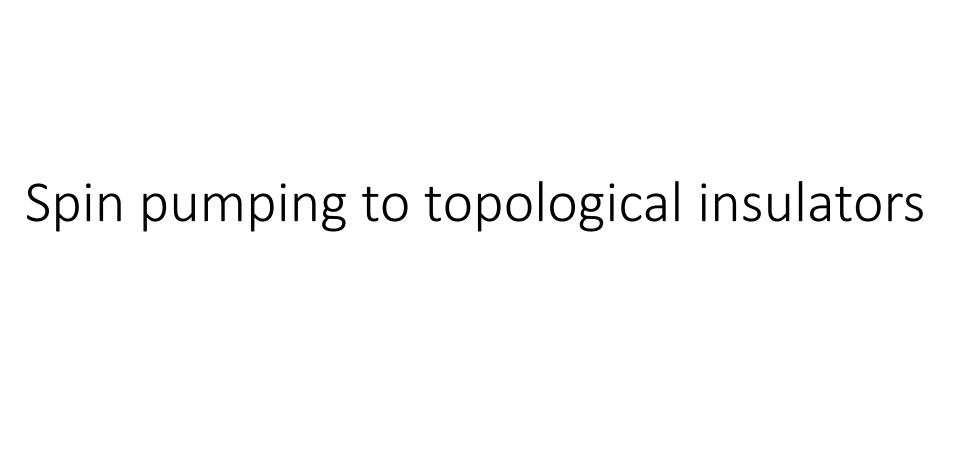


Thermal effects on FMR spectra can be serious.

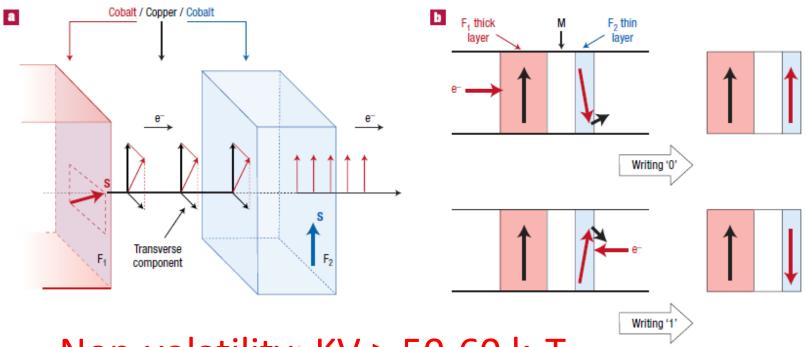
Need to change the inplane field angle to separate the spintransfer effect from the thermal effect.



Controlled sample Py/Cu: Cu has small spin Hall angle.



#### Application: data storage



Non-volatility:  $KV > 50-60 k_BT$ 

K: magnetic anisotropy constant

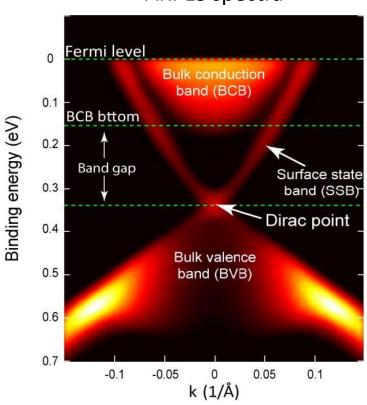
V: volume of nano-particle

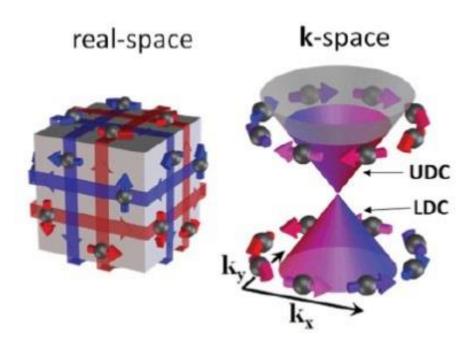
k<sub>B</sub>: Boltzmann constant

Goal: Find a material that can generate maximum spin torques from a given charge current.

#### Topological insulators

**ARPES** spectra





Nearly 100 % spin polarization.

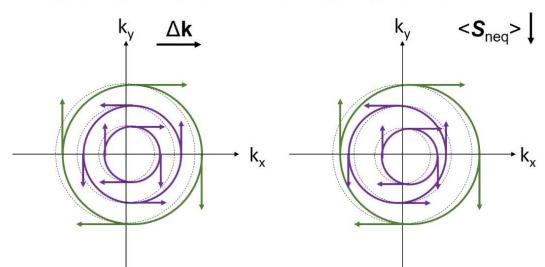
Spin-momentum locking: the direction of electron motion determines the spin direction.

#### Challenges

- Bulk conduction of TIs obscures the effect of topological surface states
- Large variation of reported effective spin Hall angle  $\theta_{\text{SH}}$  (or conversion efficiency)
  - **0.022** in Bi<sub>2</sub>Se<sub>3</sub>/Py at 15 K (Deorani et al. (2014))
  - $\sim 10^{-4}$  in bulk insulating Bi<sub>1.5</sub>Sb<sub>0.5</sub>Te<sub>1.7</sub>Se<sub>1.3</sub> at 15 K (Shiomi et al. (2014))
  - **0.021~0.43** in Bi<sub>2</sub>Se<sub>3</sub>/CoFeB at **RT** (Jamali et al. (2015))
- Current shunting effect by ferromagnetic metals in ST-FMR measurement

Ferrimagnetic insulator YIG with high thermal stability is an ideal spin source.





	Inverse spin Hall effect (ISHE)	Inverse Edelstein effect (IEE)
location	bulk	surface
condition	Spin current normal to the interface	"non-equilibrium" spin density at interface
material	Normal metals and semiconductors including 3D TIs	TIs and Rasba materials possessing k-dependent spin- polarized states

## Spin Hall angle and IEE length

 $j_c = \lambda_{IEE} j_s$  (definition of IEE length)

$$j_c = \theta_{SH} \lambda_N \, anh \left( rac{d_N}{2 \lambda_N} 
ight) j_s$$
, 2D charge current from ISHE

$$\lambda_N >> d_N, \ \lambda_{IEE} = \frac{1}{2} d_N \theta_{SH}$$

$$\lambda_N \ll d_N, \ \lambda_{IEE} = \lambda_N \theta_{SH}$$

Using spin Hall angle to determine conversion ratio of 3D  $j_c$  and 2D  $j_s$  can lead to "unphysical" value (> 1).

Ex:  $\theta_{SH}$  = 1.6 for  $\alpha$ -Sn if compared with W

#### Questions

1. Does ferromagnetic metal suppress topological surface states?

2. Can spin pumping distinguish surface and bulk effects (IEE and ISHE) of Bi<sub>2</sub>Se<sub>3</sub>?

Structure	Journal	method	Spin-charge ratio	Importance
Py Ag Bi Si (001)	Nat. Commun. <b>4</b> , 2944 (2013) (A. Fert)	Spin pumping	300K: 0.09 ~ 0.2 0.3 nm	First demonstration of RT IEE with Rasba alloys Ag/Bi
Py Bi <sub>2</sub> Se <sub>3</sub> Al <sub>2</sub> O <sub>3</sub>	Nature <b>511</b> , 449 (2014) (D. Ralph)	ST-FMR	300K: 2 ~ 3.5	Giant RT spin torque ratio of Bi <sub>2</sub> Se <sub>3</sub> "Signature" of RT EE
Py Bi <sub>2</sub> Se <sub>3</sub> Al <sub>2</sub> O <sub>3</sub>	PRB <b>90</b> , 094403 (2014) (S. Oh)	Spin pumping	300K: 0.009 15K: 0.02	ISHE of Bi <sub>2</sub> Se <sub>3</sub>
Bi <sub>2</sub> Se <sub>3</sub> , BSTS, and Sn-BTS	PRL <b>113</b> , 196601 (2014) (E. Saitoh)	Spin pumping	15K: ~10 <sup>-4</sup>	Low T IEE of TIs (crystal)
$Co_{40}Fe_{40}B_{20}$ $Bi_2Se_3$ $Al_2O_3$	PRL <b>114</b> , 257202 (2015) (S. Oh)	ST-FMR	300K: 0.047 50K: 0.42	Large Low T spin torque ratio of Bi <sub>2</sub> Se <sub>3</sub> "Signature" of RT EE

Structure	Journal	method	Spin-charge ratio	Importance
Py  Bi <sub>2</sub> Se <sub>3</sub> Co <sub>50</sub> Fe <sub>50</sub>	Sci. Rep. <b>5</b> , 7907 (2015) (University of Oxford)	Spin pumping		Atypical thickness dependence of mixing conductance
$Co_{20}Fe_{60}B_{20}$ $Bi_2Se_3$ $InP$	Nano Lett. <b>15</b> , 7126 (2015) (Jian-Ping Wang, University of Minnesota)	Spin pumping	300K: 0.43	Giant RT ISHE of Bi <sub>2</sub> Se <sub>3</sub>
Fe Ag Sn InSb (001)	PRL <b>116</b> , 096602 (2016) (A. Fert)	Spin pumping	300K: 0.62 ~ 1.5 2.1 nm	Giant RT IEE of TI Sn
$Py$ $Bi_{2}Te_{3}$ $Al_{2}O_{3}$	Submitted to PRB (S. F. Lee)	Spin pumping	5 K: 0.003 ~ 0.0062	"Signature" of low T IEE of Bi <sub>2</sub> Te <sub>3</sub> Low T ISHE of Bi <sub>2</sub> Te <sub>3</sub>
Bi <sub>2</sub> Se <sub>3</sub> YIG GGG	(our work)	Spin pumping		"Signature" of RT IEE of Bi <sub>2</sub> Se <sub>3</sub> First study on FI/TI

Structure	Journal	method	Spin-charge ratio	Importance
Ру	PRB <b>90</b> , 094403 (2014) (S. Oh)	Spin pumping	300K: 0.009 15K: 0.02	ISHE of Bi <sub>2</sub> Se <sub>3</sub>
Bi <sub>2</sub> Se <sub>3</sub>				
$Al_2O_3$				

PHYSICAL REVIEW B 90, 094403 (2014)

#### Observation of inverse spin Hall effect in bismuth selenide

Praveen Deorani, Jaesung Son, Karan Banerjee, Nikesh Koirala, Matthew Brahlek, Seongshik Oh, and Hyunsoo Yang 1,\*

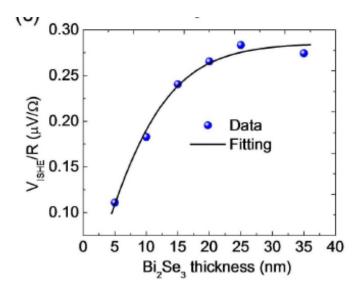
1 Department of Electrical and Computer Engineering, National University of Singapore, 117576, Singapore

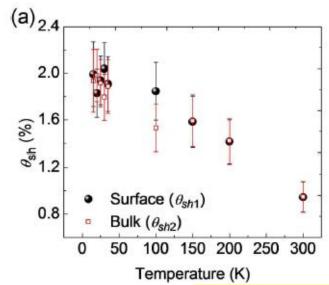
2 Department of Physics & Astronomy, Rutgers Center for Emergent Materials, Institute for Advanced Materials,

Devices and Nanotechnology, The State University of New Jersey, New Jersey 08854, USA

(Received 19 April 2014; revised manuscript received 20 August 2014; published 3 September 2014)

Bismuth Selenide ( $Bi_2Se_3$ ) is a topological insulator exhibiting helical spin polarization and strong spin-orbit coupling. The spin-orbit coupling links the charge current to spin current via the spin Hall effect (SHE). We demonstrate a  $Bi_2Se_3$  spin detector by injecting the pure spin current from a magnetic permalloy layer to a  $Bi_2Se_3$  thin film and detect the inverse SHE in  $Bi_2Se_3$ . The spin Hall angle of  $Bi_2Se_3$  is found to be 0.0093  $\pm$  0.0013 and the spin diffusion length in  $Bi_2Se_3$  to be 6.2  $\pm$  0.15 nm at room temperature. Our results suggest that topological insulators with strong spin-orbit coupling can be used in functional spintronic devices.





was taken to be of opposite signs. Fitting the measured data, we obtain  $\theta_{sh1}$  at surface and  $\theta_{sh2}$  at bulk for each temperature as shown in Fig. 4(a), which does not show any clear distinction between the surface and bulk value. Figure 4(b) shows the  $\lambda_{sf}$ 

In order to distinguish the surface and bulk contributions, they assumed a spin Hall angle  $\theta_{sh1}$  for TSS, believing that TSS would give far larger spin Hall angle than the bulk. However, the fitting results show that  $\theta_{sh1} \approx \theta_{sh2}$ . That is, no TSS features were revealed in this work.

Structure		Journal	method	Spin-charge ratio	Importance
Ру		PRL <b>113</b> , 196601 (2014) (E. Saitoh)	Spin pumping	15K: ~10 <sup>-4</sup>	Low T IEE of TIs (crystal)
Bi <sub>2</sub> Se <sub>3</sub> , BSTS, and Sn-BTS					
PRL 11	<b>3,</b> 196601	(2014) PHYSICAL R	EVIEW LETTE		ek ending EMBER 2014

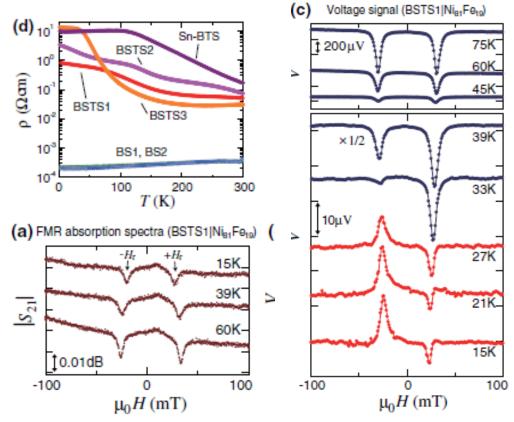
#### Spin-Electricity Conversion Induced by Spin Injection into Topological Insulators

Y. Shiomi, K. Nomura, Y. Kajiwara, K. Eto, M. Novak, Kouji Segawa, Yoichi Ando, and E. Saitoh K. Saitoh <sup>1</sup>Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan <sup>2</sup>Institute of Scientific and Industrial Research, Osaka University, Ibaraki, Osaka 567-0047, Japan <sup>3</sup>WPI Advanced Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan <sup>4</sup>CREST, Japan Science and Technology Agency, Tokyo 102-0076, Japan <sup>5</sup>Advanced Science Research Center, Japan Atomic Energy Agency, Tokai 319-1195, Japan (Received 11 May 2014; published 3 November 2014)

We report successful spin injection into the surface states of topological insulators by using a spin pumping technique. By measuring the voltage that shows up across the samples as a result of spin pumping, we demonstrate that a spin-electricity conversion effect takes place in the surface states of bulk-insulating topological insulators Bi<sub>1.5</sub>Sb<sub>0.5</sub>Te<sub>1.7</sub>Se<sub>1.3</sub> and Sn-doped Bi<sub>2</sub>Te<sub>2</sub>Se. In this process, the injected spins are converted into a charge current along the Hall direction due to the spin-momentum locking on the surface state.

DOI: 10.1103/PhysRevLett.113.196601 PACS numbers: 72.25.Pn, 72.25.Dc, 73.20.-r, 75.76.+j

Obviously, they have realized the difficulties of separating surface and bulk effects. So they choose bulk-insulating BSTS to rule out ISHE. However, the very small spincharge ratio is very puzzling. (Question 1)



The data show negative field shifts as T became lower, similar to Faris' data. However, they did not mention this.

unit vector perpendicular to the plane. Here, due to the strictly 2D nature, spins do not "flow" along the z direction within the surface state and the converted charge current  $J_c$  has the 2D nature. Hence, the mechanism of this spin-electricity conversion is different from that in the inverse spin Hall effect, where a spin current flowing within a finite thickness of a sample is converted into a 3D charge current along the Hall direction.

samples [Fig. 3(a)]. It is worth mentioning that the present spin-electricity conversion effect is rather similar to that reported in Rashba-split systems [31,32], but the efficiency is, in principle, much higher in TIs than that in the Rashba-split system [33]. The spin-momentum locking on a single Dirac cone predicts efficient spin-electricity conversion in TIs even at room temperature as long as the surface state is robust, while in the Rashba-split systems where a pair of bands exist, one of the bands counteracts the effect of the other.

#### The thing is, are TSS still "robust" in this structure?

to the spin-momentum locking. Though the efficiency of the spin-electricity conversion in the present work is as small as  $\eta \sim 10^{-4}$ , the spin-momentum locking on topological surface states can, in principle, lead to efficient conversion between spin and electricity.

Structure	Journal	method	Spin-charge ratio	Importance
$Co_{20}Fe_{60}B_{20}$ $Bi_2Se_3$	Nano Lett. <b>15</b> , 7126 (2015) (Jian-Ping Wang, University of Minnesota)	Spin pumping	300K: 0.015 ~ 0.43	Giant RT ISHE of Bi <sub>2</sub> Se <sub>3</sub>
InP				



Letter

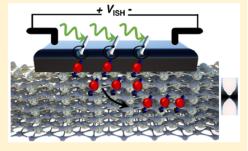
pubs.acs.org/NanoLett

#### Nothing new in physics again.

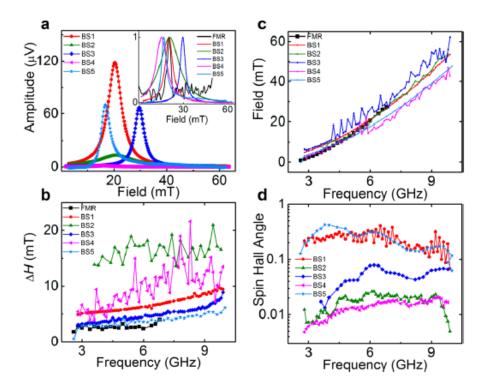
#### Giant Spin Pumping and Inverse Spin Hall Effect in the Presence of Surface and Bulk Spin—Orbit Coupling of Topological Insulator Bi<sub>2</sub>Se<sub>3</sub>

Mahdi Jamali,<sup>†</sup> Joon Sue Lee,<sup>‡</sup> Jong Seok Jeong,<sup>§</sup> Farzad Mahfouzi,<sup>||</sup> Yang Lv,<sup>†</sup> Zhengyang Zhao,<sup>†</sup> Branislav K. Nikolić,<sup>⊥</sup> K. Andre Mkhoyan,<sup>§</sup> Nitin Samarth,<sup>\*,‡</sup> and Jian-Ping Wang<sup>\*,†</sup>

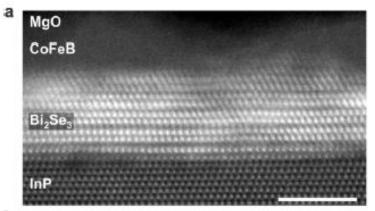
ABSTRACT: Three-dimensional (3D) topological insulators are known for their strong spin—orbit coupling (SOC) and the existence of spin-textured surface states that might be potentially exploited for "topological spintronics." Here, we use spin pumping and the inverse spin Hall effect to demonstrate successful spin injection at room temperature from a metallic ferromagnet (CoFeB) into the prototypical 3D topological insulator Bi<sub>2</sub>Se<sub>3</sub>. The spin pumping process, driven by the magnetization dynamics of the metallic ferromagnet, introduces a spin current into the topological insulator layer, resulting in a broadening of the ferromagnetic resonance (FMR) line width. Theoretical modeling of spin pumping through the surface of Bi<sub>2</sub>Se<sub>3</sub>, as well as of the measured angular dependence of spin-charge conversion signal, suggests that pumped spin current is first greatly



enhanced by the surface SOC and then converted into a dc-voltage signal primarily by the inverse spin Hall effect due to SOC of the bulk of  $Bi_2Se_3$ . We find that the FMR line width broadens significantly (more than a factor of 5) and we deduce a spin Hall angle as large as 0.43 in the  $Bi_2Se_3$  layer.



The samples had severely degraded. All of the curves should be smooth, so the calculated spin Hall angles are questionable.



The wide fluctuation of spin pumping signals from sample to sample could be explained based on the nonuniform composition of Bi<sub>2</sub>Se<sub>3</sub> at its interface with the magnetic layer. Recently, it has been shown that surfaces of TIs are very nonuniform in terms of chemical potential and position of Dirac point.<sup>53</sup> Because the Bi<sub>2</sub>Se<sub>3</sub>/CoFeB interface plays the major role in the spin injection, the large variations of the spin pumping characteristics could be associated with nonuniform Bi<sub>2</sub>Se<sub>3</sub> surface. Moreover, the decapping process could also be responsible for modification of the TI surface considering Bi<sub>2</sub>Se<sub>3</sub> has strong thermoelectric properties.<sup>54</sup> Comparing the samples BS1-4 with BS5, BS5 is not involved in any hightemperature decapping process and we obtain the maximum spin Hall angle in this sample. This suggests that heat treatment temperature and a large spin Hall angle. In highly bulkconductive Bi<sub>2</sub>Se<sub>3</sub> TIs, the inverse Hall effect of the bulk seems to dominate over the inverse Edelstein effect of the surface state, at least in spin pumping experiments. Moreover, we find

(Question 2??)

Structure	Journal	method	Spin-charge ratio	Importance
Fe	PRL <b>116</b> , 096602 (2016)	Spin pumping	300K: 0.62 ~ 1.5	Giant RT IEE of TI Sn
Ag Sn InSb (001)	(A. Fert)		2.1 nm	

PRL 116, 096602 (2016)

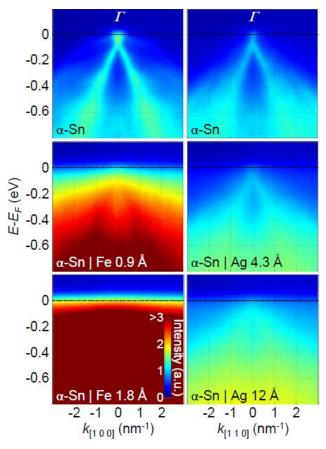
PHYSICAL REVIEW LETTERS

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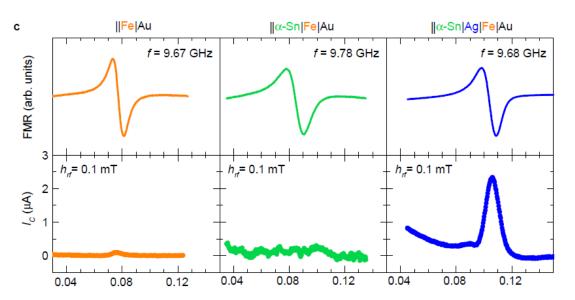
#### Spin to Charge Conversion at Room Temperature by Spin Pumping into a New Type of Topological Insulator: α-Sn Films

J.-C. Rojas-Sánchez, <sup>1,\*</sup> S. Oyarzún, <sup>2,3</sup> Y. Fu, <sup>2,3</sup> A. Marty, <sup>2,3</sup> C. Vergnaud, <sup>2,3</sup> S. Gambarelli, <sup>2,3</sup> L. Vila, <sup>2,3</sup> M. Jamet, <sup>2,3</sup> Y. Ohtsubo, <sup>4,5</sup> A. Taleb-Ibrahimi, <sup>6,7</sup> P. Le Fèvre, <sup>7</sup> F. Bertran, <sup>7</sup> N. Reyren, <sup>1,†</sup> J.-M. George, <sup>1</sup> and A. Fert <sup>1</sup>Unité Mixte de Physique, CNRS, Thales, Univ. Paris-Sud, Université Paris-Saclay, 91767 Palaiseau, France <sup>2</sup>Université Grenoble Alpes, INAC-SP2M, F-38000 Grenoble, France <sup>3</sup>CEA, Institut Nanosciences et Cryogénie, F-38000 Grenoble, France <sup>4</sup>Graduate School of Frontier Biosciences, Osaka University, Suita 565-0871, Japan <sup>5</sup>Graduate School of Science, Osaka University, Toyonaka 560-0043, Japan <sup>6</sup>UR1 CNRS, Synchrotron SOLEIL, Saint-Aubin, 91192 Gif sur Yvette, France <sup>7</sup>Synchrotron SOLEIL, Saint-Aubin, 91192 Gif sur Yvette, France (Received 18 December 2015; published 1 March 2016)

We present results on spin to charge current conversion in experiments of resonant spin pumping into the Dirac cone with helical spin polarization of the elemental topological insulator (TI)  $\alpha$ -Sn. By angle-resolved photoelectron spectroscopy (ARPES), we first check that the Dirac cone (DC) at the  $\alpha$ -Sn (0 0 1) surface subsists after covering Sn with Ag. Then we show that resonant spin pumping at room temperature from Fe through Ag into  $\alpha$ -Sn layers induces a lateral charge current that can be ascribed to the inverse Edelstein effect by the DC states. Our observation of an inverse Edelstein effect length much longer than those generally found for Rashba interfaces demonstrates the potential of TIs for the conversion between spin and charge in spintronic devices. By comparing our results with data on the relaxation time of TI free surface states from time-resolved ARPES, we can anticipate the ultimate potential of the TI for spin to charge conversion and the conditions to reach it.



Fermi level is very closed to the Dirac point of Sn. TSS disappeared when Fe was deposited on top. (Question 1)



surfaces" of  $TI^{22}$ . We believe that the long relaxation time on free topological surfaces characterizes the slow relaxation inside the 2D topological states whereas, by interfacing the TI (or Rashba) surface with a metal as Ag, we introduce a faster additional relaxation mechanism provided by exchanges of electrons with the adjacent 3D metal. We conclude that the best conditions for the exploitation of topological sates of TI in spintronics should be with TI interfaced with (trivial) insulators instead of metals, for example in experiments of spin-pumping or thermal<sup>23</sup> spin injection from an insulating ferromagnet. If one remarks that  $v_F \tau$  is also the critical length for

Could this explain the small spin-charge ratio from the Japanese group's work?

Structure		Journal	method	Spin-charge ratio	Importance
Ру		Nature <b>511</b> , 449 (2014) (D. Ralph)	ST-FMR	300K: 2 ~ 3.5	Giant RT spin torque ratio of  Bi <sub>2</sub> Se <sub>3</sub> "Signature" of RT EE
Bi <sub>2</sub> Se <sub>3</sub>					
Al <sub>2</sub> O <sub>3</sub>					

#### LETTER

doi:10.1038/nature13534

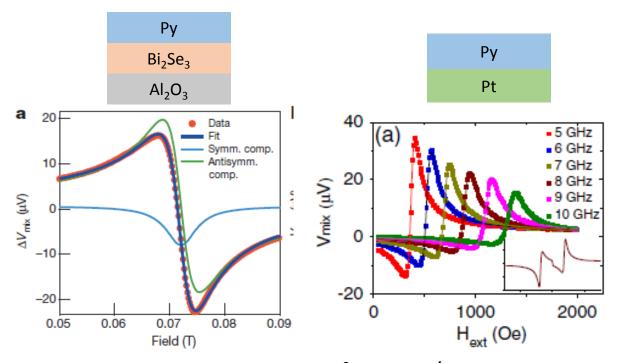
## Spin-transfer torque generated by a topological insulator

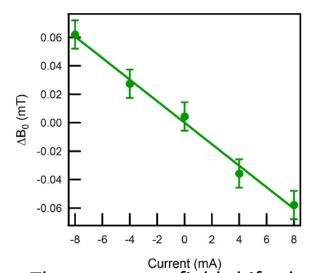
A. R. Mellnik<sup>1</sup>, J. S. Lee<sup>2</sup>, A. Richardella<sup>2</sup>, J. L. Grab<sup>1</sup>, P. J. Mintun<sup>1</sup>, M. H. Fischer<sup>1,3</sup>, A. Vaezi<sup>1</sup>, A. Manchon<sup>4</sup>, E.-A. Kim<sup>1</sup>, N. Samarth<sup>2</sup> & D. C. Ralph<sup>1,5</sup>

#### Signatures of Edelstein effect (EE):

- 1. Large anti-symmetric component of voltage signals.
- 2. Resonance field shifts.

The two features result from non-equilibrium spin density at TSS.





The resonance field shifted when applying dc current. From the shifts, magnitude of field-like torques can be determined.

Large antisymmetric component for Bi<sub>2</sub>Se<sub>3</sub>/Py. In contrast, symmetric signals dominate for Pt/Py (without EE).

any previously measured spin current source material. However, as noted above, for practical applications the specific layer structure of our devices (topological inculator/matellia magnet) does not make good use of this

high intrinsi

through the

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insulator. Using insulating magnets may also have the advantage of providing much less Gilbert damping than do metallic magnets<sup>29</sup>, which

They did not do Bi<sub>2</sub>Se<sub>3</sub> thickness dependence measurement, so it's still hard to extract the EE.

resent for ma-Additionally, ing of bilayer eliminate any

magnets so that the majority of the current will flow in the topological

deleterious effects of bulk conduction. Our results therefore point towards

Structure	Journal	method	Spin-charge ratio	Importance
$Co_{40}Fe_{40}B_{20}$ $Bi_{2}Se_{3}$ $Al_{2}O_{3}$	PRL <b>114</b> , 257202 (2015) (S. Oh)	ST-FMR	300К: 0.047 50К: 0.42	Large Low T spin torque ratio of Bi <sub>2</sub> Se <sub>3</sub> "Signature" of RT EE

PRL 114, 257202 (2015)

PHYSICAL REVIEW LETTERS

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#### Topological Surface States Originated Spin-Orbit Torques in Bi<sub>2</sub>Se<sub>3</sub>

Yi Wang, <sup>1</sup> Praveen Deorani, <sup>1</sup> Karan Banerjee, <sup>1</sup> Nikesh Koirala, <sup>2</sup> Matthew Brahlek, <sup>2</sup> Seongshik Oh, <sup>2</sup> and Hyunsoo Yang <sup>1,\*</sup>

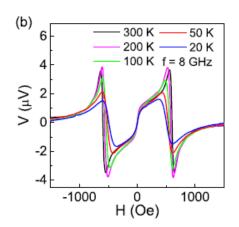
<sup>1</sup>Department of Electrical and Computer Engineering, National University of Singapore, 117576 Singapore, Singapore

<sup>2</sup>Department of Physics and Astronomy, Rutgers, The State University of New Jersey, Piscataway, New Jersey 08854, USA

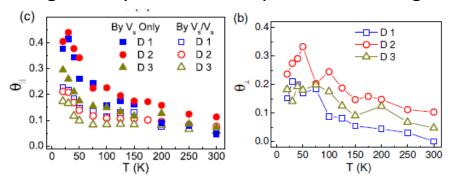
(Received 4 February 2015; revised manuscript received 27 April 2015; published 24 June 2015)

The three dimensional topological insulator bismuth selenide ( $Bi_2Se_3$ ) is expected to possess strong spin-orbit coupling and spin-textured topological surface states and, thus, exhibit a high charge to spin current conversion efficiency. We evaluate spin-orbit torques in  $Bi_2Se_3/Co_{40}Fe_{40}B_{20}$  devices at different temperatures by spin torque ferromagnetic resonance measurements. As the temperature decreases, the spin-orbit torque ratio increases from  $\sim 0.047$  at 300 K to  $\sim 0.42$  below 50 K. Moreover, we observe a significant out-of-plane torque at low temperatures. Detailed analysis indicates that the origin of the observed spin-orbit torques is topological surface states in  $Bi_2Se_3$ . Our results suggest that topological insulators with strong spin-orbit coupling could be promising candidates as highly efficient spin current sources for exploring the next generation of spintronic applications.

DOI: 10.1103/PhysRevLett.114.257202 PACS numbers: 75.76.+j, 72.25.Dc, 73.20.-r, 85.75.-d



Large antisymmetric component of voltage.



Spin-charge ratio was greatly enhanced at low T. But the RT values are two order of magnitudes smaller than that from the Cornell group.

On the other hand, a possible out-of-plane spin polarization in the TSS has been theoretically predicted [55,56] and experimentally observed in Bi<sub>2</sub>Se<sub>3</sub> [57,58], which is attributed to the hexagonal warping effect in the Fermi surface [55,59]. This out-of-plane spin polarization in the TSS can account for the observed  $\Delta \tau$  especially in the low temperature range (<50 K), and the  $\Delta \tau$  adds to the  $\tau_{Oe}$  [27,31]. Moreover, as shown in Figs. 3(a) and 4(a), the out-of-plane torque ( $\Delta \tau$ ) has the same order of magnitude comparable to the in-plane torque ( $\tau_{\parallel}$ ) below 50 K ( $\Delta \tau/\tau_{\parallel} \sim 60\%$ ) [37], which is in agreement with the behavior of hexagonal TSS in TI [55,56]. With the analysis from different aspects, our findings especially in the low temperature range (<50 K) indicate a TSS origin of spin-orbit torques in Bi<sub>2</sub>Se<sub>3</sub> and CFB.

They explained the origin of field-like torques with spin texture only qualitatively. They did not resort to the model proposed by the Cornell group.

#### Questions

1. Does ferromagnetic metal suppress topological surface states?

Yes. (A. Fert and E. Saitoh)

2. Can spin pumping distinguish surface and bulk effects (IEE and ISHE) of Bi<sub>2</sub>Se<sub>3</sub>?

It's difficult for TI/FM, but how about FI/TI?

3. Now that ST-FMR have shown the signature of EE with large field-like torques, which come from non-equilibrium spin density, is it possible to observe similar effect (IEE) with spin pumping?

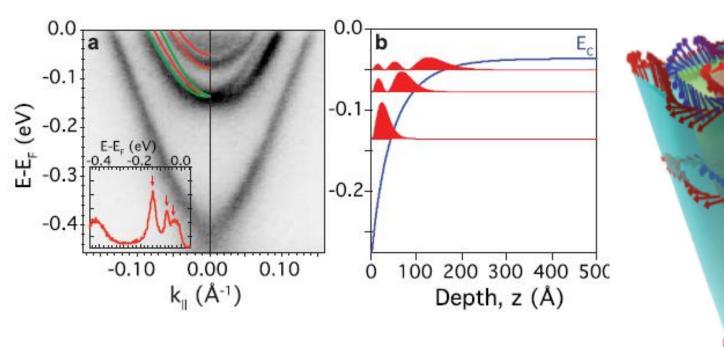
Note that in A. Fert's work they did not deposit Fe directly on Sn. A Ag layer may weaken the effect of non-equilibrium spin density, which is localized, on Fe. That is, the Ag layer separate Fe and Sn out of the range of exchange coupling. Therefore, "signatures (negative field shift)" of IEE were not observed.

#### More questions

 How does the ac component of the pumped spin current affect the TSS?

 How does spin canting of TSS affect the spin transport properties?

#### Spin texture of Bi<sub>2</sub>Se<sub>3</sub>



- ➤ Large Rashba splitting of 2DEG in Bi<sub>2</sub>Se<sub>3</sub> has been confirmed by ARPES. The interplay between TSS and 2DEG leads to intricate spin texture.
- The spin pumping effect strongly depends on the interface electronic structure and spin texture.
- ➤ The spin transport of topological interface state near a magnetic layer is of further interest to investigate.